

## *Stat 134: Section 11*

*Brett Kolesnik*

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### ***Conceptual Review***

Please discuss these short questions with those around you in section. These problems are intended to highlight concepts from lecture that will be relevant for today's problems.

- a. What is the Taylor expansion of  $e^x$ ?
- b. If  $X \sim \text{Pois}(\lambda)$  on  $\{0, 1, 2, \dots\}$ , what is  $P(X = x)$ ?

### *Problem 1*

Prove that mean and variance of the Poisson distribution with parameter  $\lambda$  are both  $\lambda$ .

*Problem 2*

Suppose  $X, Y$ , and  $Z$  are independent Poisson random variables, with parameters  $\mu_X, \mu_Y, \mu_Z$  respectively. Find:

- a.  $P(X + Y) = 4$
- b.  $E[(X + Y + Z)^2]$

*Problem 3*

Let  $X$  have Poisson ( $\lambda$ ) distribution. Calculate:

- a.  $E(3X + 5)$
- b.  $Var(3X + 5)$
- c.  $E[\frac{1}{1+X}]$