

Warmon: 10:00-1910 Recall that the commutative distribution function (CDF) for a RV X is F(x)=P(XEx) Dran the CDF for each of the distrikitions below? Slope b-a **H**er EX~UnH(a,b) f(x) <u>)</u> b-a -۲ b a Ex Xn Bernoull! (P=16) **H**er ·6 (·6) -f(x) .4 - X + ۲ 1-e-2+ 些TへExpla Ft FH $P(T_{7+1}) = e^{-\lambda t}$ $- F(*) = P(T_{2+1}) = 1 - e^{-\lambda t}$ t-24 -2e Today (i) review MGF E)sec 4.5 Find CDF of a mixed distribution

(3) sec 4.5 Using CDF to find E(X)

(1) Review M6F

$$X RV_{, t} \in R$$

 $M_{, t} = E(e^{tX})$
 $E \times n Gamma(r, \lambda)$ Variable part
 $f_{, (x)} = \frac{1}{2} \cdot \frac{1}{x^{-1}} \cdot \frac{1}{x^{-1}} \cdot \frac{1}{x^{-2}} \cdot \frac{1}{x^{$

Knowing the MGF uniquely specifies the distribution

And

Stat 134 Monday April 1 (CDP

1. Let X have density $f(x) = xe^{-x}$ for x > 0. The MGF is? **a** $M_X(t) = \frac{1}{1-t}$ for t < 1 **b** $M_X(t) = \frac{1}{(1-t)^2}$ for t < 1 **c** $M_X(t) = \frac{1}{(1+t)^2}$ for t > -1**d** none of the above

(2) sec 4.5 CDF of where distributions



Suppose you are trying to discretly leave a party. Your time to leave is uniform from 0to 2 minutes. However, if your walk to the exit takes more than 1 minute, you run into a friend at the door and and must spend the full 2 minutes to leave. Let T represent the time it takes you to leave. True or false the graph of the cdf of T is: F(4) 5 F(+) ft Т 2 valkin **f**lla note th 4 5 Z a jump q 6=2





Note: doesn't have to be continuous RV.



Thus (1522) Prod at and other
Let X have CDF F.
Then the RV F'(U) = X
U
then the RV F'(U) = X
How is this useful to us finding E(X)?
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$$E(X) = E(F'(U)) = \int_{0}^{1} F(U)F(U) dU$$

Notice
X
Notice
X
 $\int_{0}^{1} \frac{1}{1} F(U)$
Now reliest
the above graph
above the
diagonal y=X
U
 $\int_{0}^{1} F(X)$
 $F(X)$
 $f($

we can find the shaded regton by integrating I-F(x) with respect to X:

The Let X be a Pos. render variable,
with CDF F. (continues, discrete, mixed),

$$E(X) = \int (1 - F(x)) dX + \frac{t(x)}{r} F(x)$$

 $F(x) = \int (1 - F(x)) dX + \frac{t(x)}{r} F(x)$
 $F_{T}(x) = 1 - e^{-\lambda t}$
Calculate $E(T)$.
 $E(T) = \int (1 - F(x)) dt = \int e^{-\lambda t} e^{-\lambda t} e^{-\lambda t} \int e^{-\lambda t} e^{-\lambda t} e^{-\lambda t} \int e^{-\lambda t} e^{-\lambda t} e^{-\lambda t} e^{-\lambda t} \int e^{-\lambda t} e^{-\lambda t} e^{-\lambda t} e^{-\lambda t} \int e^{-\lambda t} e^{-\lambda t}$

the is sometimes eacher to calculate E(X) using the cold (avoid doing integration by parts): E(T) = Stherdt

25

Suppose you are trying to discretly leave a party. Your time to leave is uniform from 0 to 2 minutes. However, if your walk to the exit takes more than 1 minute, you run into a friend at the door and and must spend the full 2 minutes to leave. Let T represent the time it takes you to leave. True or false, the graph of the cdf of T is: $F \rightarrow E(T)$

E(T)=.75+,5=1,25

Append:x ~ See P 322 in book Claim for any CDF F X = F'(U) is a RV with cdf F. Proo L/ let X = F'(U) $F(\kappa) = P(X \leq \kappa) \quad \text{we will show} \\ F_{X} = F$ = P(F'(U) = x) =P(FF(U) = F(x)) Since F is increasing $= \mathcal{P}(\cup \leq f(x))$ - F(x) silve P(UE)=0