

## Stat 134: Section 16

Adam Lucas

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### Conceptual Review

Let  $(X, Y)$  has joint density  $f(x, y)$

- How can we tell from the density function that  $X, Y$  are independent?
- How do we find  $P(A)$  for  $A \subset \mathbb{R}^2$ ?
- Now assume  $X, Y$  are independent standard Gaussian random variables. What can we say about  $aX + bY + c$ ?

### Problem 1

Let  $X$  and  $Y$  have joint density

$$f(x, y) = \begin{cases} 20(y - x)^3 & 0 < x < y < 1 \\ 0 & \text{otherwise} \end{cases}$$

- Find  $P(Y > 2X)$ .
- Find the marginal density of  $X$ .

*Problem 2*

Let  $X$  and  $Y$  have joint density

$$f(x, y) = \frac{1}{2\pi} \exp \left[ -\frac{1}{2}(x^2 + y^2) \right] \left\{ 1 + xy \exp \left[ -\frac{1}{2}(x^2 + y^2 - 2) \right] \right\}.$$

- a. Find marginal density of  $X$  and  $Y$ .
- b. Conclude that even when marginal density of  $X, Y$  are Gaussian,  $(X, Y)$  may not be jointly Gaussian.