

## *Stat 134: Section 17*

*Adam Lucas*

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### *Conceptual Review*

- a. What is p.d.f of the normal  $(0, 1)$  distribution? Use the change of variable formula to also find p.d.f of normal  $(\mu, \sigma^2)$  distribution.
- b. If  $X$  and  $Y$  are independent with normal  $(\lambda, \sigma^2)$  and normal  $(\mu, \tau^2)$  distributions, then what distribution does  $aX + bY$  follow?

### *Problem 1*

Let  $X$  and  $Y$  be independent and normally distributed,  $X$  with mean 0 and variance 1,  $Y$  with mean 1. Suppose  $P(X > Y) = 1/3$ . Find the variance of  $Y$ .

*Problem 2*

Let  $Z$  be normal  $(0, 1)$  random variable. Let  $X = Z^2$ , use change of variable formula to calculate the distribution of  $X$ . Is that the distribution we already know?