Stat 134 Lec 28

1000-10:10-10:10

Let
$$X \wedge Exp(\lambda)$$
, $Y \wedge Exp(\lambda)$
(recall, $f_{X}(\lambda) = \lambda e^{-\lambda x}$)
be indevendent Difettimes of two bulbs.
Find $P(X < Y)$.
Hind: use $f(x,y) = f(x)G(x)$
 $F(x,y) = \lambda x \int e^{-\lambda x} \int e^$

Last the,
Sec 4.16 Beta Dilstillution
Let r.S > 0
P ~ Beta(r.s) it

$$f(r) = \Gamma(r+s) P^{-1}(1-p)^{1}$$
 for $O2P21$
 $\Gamma(r)\Gamma(s)$

Applications

a) Beta (r, s) taxes values between 0 and 1 and commonly models the prior distribution of a probability in Bayestan statistics.

$$\begin{array}{l} \underbrace{\bigoplus_{i=1}^{9} \underbrace{\operatorname{Siz}_{i,j=2}}_{i \in \mathbb{N}} \operatorname{Siz}_{i \in \mathbb{N$$



Not a great Picture beause the oval in green should be a clude, This is the Picture of a corrolated Liverilate normal from Chapter 6 Instead of an Uncorrelated Liverilate Normal.

$$\stackrel{\text{ex}}{=} If x, y \stackrel{\text{ild}}{\sim} U(0, 1)$$

Find $P(y \ge \ge |y \ge 1 - 2k)$
Soln

$$f(x,y) = f(x)f(y) = 1$$
 for , 0 else.

$$P(Y = \pm | Y = 1 - 2\kappa) = \frac{P(Y = \pm, Y = 1 - 2\kappa)}{P(Y = 1 - 2\kappa)}$$
 Bayes rule



$$\frac{P(Y=\frac{1}{2}, Y=1-2x)}{P(Y=1-2x)} = \frac{1/2 - 1/16}{1 - 1/4} = \frac{1}{2}/12$$

survey position of Polson random scatters:

let Nt ~ Pois (n= it) and Mt Pois (n= independent PRS corresponding to the number of avoluated red and purple caves in time t.

Competing exponentials: Let X = thre until the first red (av) Y = thre until the first purple (av)when is the chance the first (av is red? $P(X \leq Y) = \frac{\lambda_1}{\lambda_1 + \lambda_2}$

ex

(Exponential distributions) You are first in line to have your question answered by either of the 2 uGSIs, Brian and Yiming, who are busy with their current students. Your question will be answered as soon as the first uGSI finishes. The times spent with student by Brian and Yiming are independent and exponentially distributed with (positive) rates λ_B and λ_Y respectively, i.e. Brian's distribution is Exponential(λ_B), and Yiming's is Exponential(λ_Y).

(a) Find the probability that Yiming will be the one answering your questions.

 $P(\gamma \in B) = \frac{\lambda_{\gamma}}{\lambda_{\gamma} + \lambda_{\beta}}$

(b) What is the distribution of your wait time? Your answer should not include integrals.

So
$$P(Y = mln(Y,B)) = P(Y(B) = \frac{\lambda_Y}{\lambda_Y + \lambda_B}$$

If χ_1, \dots, χ_n are indep exponentials
with values $\lambda_1, \dots, \lambda_n$
 $P(\chi_i^* = mln(\chi_1, \dots, \chi_n)) = ? \qquad \lambda_i^* + \dots + \lambda_n$
Now have $E = 6SI, Ylming, Belien and Rowen.
What is chouse Yiming down first, then
Brien and then Rowen (indep exponentials
with reduce $\lambda_Y, \lambda_B, \lambda_R$)?
i.e. $P(Y < B < R)$
 $P(Y = mln(Y,B,R), B = mln(B,R) | Y = mln(Y,B,R))$
 $= P(Y = mln(Y,B,R)) \cdot P(B = mln(B,R) | Y = mln(Y,B,R))$
 $= P(Y = mln(Y,B,R)) \cdot P(B = mln(B,R) | Y = mln(Y,B,R))$$

Continuous Picture: marginal density

