Stat 134 1ec 6

Warmup 10:00-10:10

Mothather: It is difficult to calculate exact probabilities with the binomial formula. It is easier to calculate the area under the normal curve.

745 75 75.5



Suppose that each of 300 patients has a probability of 1/3 of being helped by a treatment independent of its effect on the other patients. Find approximately the probability that more than 134 patients are helped by the treatment. (Be sure to use the continuity correction. You will not receive full credit otherwise)

Hint The mean of
$$Bin(n,p)$$
 is $M = np$
The standard deviation of $Bin(np)$ is $T = \sqrt{npe}$
 $X = \#$ Pattents helped
 $P(X \ge 134.5) = 1 - \Phi(X < 134.5) = 1 - \Phi(B4.5 - 100)$
 $300(4)(4)$
 $2(-1 = 0)$

(1) Sec Z.Z Normal approximation to the bihomilal distribution





. (3 pts) Southwest overbooks its flights, knowing some people will not show up. Suppose for a plane that seats 350 people, 360 tickets are sold. Based on previous data, the airline claims that each passenger has a 90% chance of showing up. Approximately, what is the chance that at least one 1 empty seat remains? (There are no assigned seats.)

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 $\mathcal{M} = \frac{360(.7)}{500(.7)(.7)} = \frac{370}{5.7}$ X = # people who show up P(X 5 349.5) M+3JC (n L = \$\overline{(3495 - M)} M-30 20 C n > 20 L - ∲ (4,47) = 1

(2) Sec 2.4 (skip 2.3) Poisson approx to Binowial

The normal approximation has almost 100% of data ±35 from the mean M. For this reason we approximated the binomial withe normal only when ME35 is between O and N.



Then Proven in appendix at only at lecture notes,

$$\begin{array}{c} Then \\ P(P(k)) \neq^{(n)}(1,P) \xrightarrow{(n)} & \underset{k=1}{\overset{(n)}{\longrightarrow}} & \underset{k=1}{\overset{(n$$

et 97.8% of approx 30 million poor families in the US. have a foldage. If you rendomly sample 100 of these families roughly what is the chance 98 or have a foldage? Deer to bean (m) $P(K) = \underbrace{e^{m_{k}}}_{K!} for K=0,12,...$ Think about this for next time.

$$\frac{A_{prevendent}}{\text{Them let } P_{n}(\mathbf{r}) = \binom{n}{k} p^{k} (1-p)^{nk} \quad (\text{them be formula})$$

$$\frac{P_{p}(\mathbf{r}) p^{k}(1-p)}{P_{p}(\mathbf{r}) p^{k}(1-p)} \xrightarrow{e^{-M} r} \xrightarrow{k} as n \to \infty \text{ and } p \to 0$$

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$$\frac{P_{p}(\mathbf{r}) p^{k}(1-p)}{P_{p}(\mathbf{r}) p^{k}(1-p)} \xrightarrow{k} \frac{P_{p}(\mathbf{r}-1) p^{k}}{K}$$

$$\frac{P_{p}(\mathbf{r}) p^{k}(\mathbf{r}) p^{k}(\mathbf{r}) p^{k}(\mathbf{r}) p^{k}(\mathbf{r}) \xrightarrow{k} p^{k}(\mathbf{r}) p^{k}$$

Proof of fact(Z):

$$P_{n}(K) = P_{n}(K-1) \underbrace{M}_{K}$$
Proof of fact(Z):

$$P_{n}(K) = P_{n}(K-1) \underbrace{P_{n}(K-1)}_{K} = \underbrace{\left[\underbrace{N-K+1}{K} \right] \frac{P}{2}}_{n(K-1)}$$

$$= P_{n}(K-1) \underbrace{\left[\underbrace{n-(K-1)}{K} \right] \frac{P}{2}}_{K}$$

$$= P_{n}(K-1) \underbrace{\left[\underbrace{n-(K-1)}{K} \right] \frac{P}{2}}_{K} \approx P_{n}(K-1) \underbrace{M}_{K}$$