warmup:

A drawer contains s black socks and s white socks (s> 0). I pull two socks out at random without replacement and call that my first pair. Then I pull out two socks at random without replacement and call that my second pair. I proceed in this way until I have s pairs and the drawer is empty. Find the expected number of pairs in which two socks are different colors.

$$X = \text{Number of pairs (out et S) of misuratches.}$$
 $T_2 = \{1 \text{ if } 2^{\text{NR}} \text{ pqi/ is misuratches.}$
 $P = 2.3.5 \text{ change set } 2^{\text{NR}} \text{ properties of the propert$

Last time sec 3.2 Expectation

 $E(x) = \begin{cases} x P(x=x) \end{cases}$

If X is a count, X can be written as

a sum of indicators

Som of indicators $X = T_1 + T_2 + \cdots + T_n, \quad T'_s = \begin{cases} 1 & \text{Prob } p \\ 0 & \text{prob } 1-p \end{cases}$ $E(\Xi_i) = 1.P + 0.(1-P) = P$

Idea Even It indicators are dependent the expectation of each indicator is an unconditional bepopepjijti.

Try Choosing indicators such that all indicates have the some expectation P.

then E(x) = n.p

we fromed it X~Bin (n,p) => E(x) =np

if X~ HG(n,N,6) => E(x)=nG

Ex X= # aces in a porer hand from a deck

 $\times \wedge HG(n, N, 6) = 4$

X= I, +I2 + I3 + I4 + T5

Iz= { 1 H 2 cand 12 on ace / P= 4/52

 $E(x) \approx 5$, $E(I_1) = 5$, $\left(\frac{4}{5}\right)$

O SEC 3.2 More expectation with Indicator examples

U sec 3.2 talksom formula

(1) Sec 3.2 more expectation/indicato- examples er Consider a 5 card deck consisting of 2,7,3,4,5 shake te cares. Let X = number of cords before the first Z a) what are the range of values of X? 0, 1, 7, 3 b) unite x as a sum of indicadors X = Iz+Iy+Is c) How is an indicator defined. P Iz= SIH 3 before that 2 d) Find E(I3)

Note to position of have a 3 in it.

y and 5 to incleven. 2 2 2 e) Find E(x)

you can not 3 E(X) = E(Is) + E(Is) = []

1/2

1/2

1/3

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Stat 134

- 1. Consider a well shuffled deck of cards. The expected number of cards before the first ace is?
 - a 52/5
 - **b** 48/5
 - **c** 48/4
 - d none of the above

$$X = I_1 + I_2 + \dots + I_{48}$$

$$I_2 = \begin{cases} 1 & \text{if } 2^{48} \\ \text{order} \end{cases}$$

$$-A_1 - A_2 - G_3 - A_4 - G_4 - G_5 \end{cases}$$

$$P = \frac{1}{3} \text{ show 5 equally likely slots}$$

$$\text{He second varace can } g_0,$$

$$E(k) = \frac{1}{3} (\frac{1}{3})$$

$$= \frac{1 \cdot P(\kappa = 1) + 2 \cdot P(\kappa = 2) + \cdots}{P_2}$$

This is useful when it is easy to find P(XZK)

A fail die is rolled 10 Homes.

Let X=max(X1,11,X10)

Fird E(K)

$$P(x \ge t) = 1 - P(x < k)$$

$$= 1 - P(x_1 < k) P(x_2 < k) ..., Y_{10} < k)$$

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= 1-
$$(\frac{\kappa-1}{6})^{10}$$
 for 15 K 5 6

$$e^{-\frac{1}{2}} \left[-\frac{\binom{9}{7}}{\binom{1}{2}} + \frac{1 - \binom{9}{2}}{\binom{1}{2}} + \frac{1 - \binom{9}{2}}{\binom{1}{2}} + \frac{9}{2} + \frac{9$$

$$= \theta - (\frac{\theta}{10}) \left[1_{10} + S_{10} + 3_{10} + A_{10} + 2_{10} \right] = (2.85)$$

(b) Find E (min(x, x2, x3))

P(min 21) + P(min 22) + ... + V(min 26)

P(x, 21)³ (x, 22)³ (x, 26)⁵

=
$$1^3 + (\frac{\pi}{6})^3 +$$

Let Y be the sum of the largest Z numbers. Notice that $Y = X_1 + X_2 + X_3 - mln(X_1, X_2, X_3)$

extra problem

. (3 pts) On a telephone wire, n birds sit arranged in a line. A noise startles them, causing each bird to look left or right at random. Calculate the expected number of birds which are not seen by an adjacent bird.

$$X = \# \text{ blids not seen by en}$$

$$x = T, + Tz + \dots + Tn$$

$$T_1 = \begin{cases} 1 & \text{if } 1 \\ \text{odiaceut bird} \end{cases}$$

$$T_2 = \begin{cases} 1 & \text{if } 1 \\ \text{odiaceut bird} \end{cases}$$

$$T_3 = \begin{cases} 1 & \text{if } 1 \\ \text{odiaceut bird} \end{cases}$$

$$T_4 = \begin{cases} 1 & \text{if } 1 \\ \text{odiaceut bird} \end{cases}$$

$$P = \begin{cases} 1 & \text{if } 1 \\ \text{odiaceut bird} \end{cases}$$

$$P = \begin{cases} 1 & \text{if } 1 \\ \text{odiaceut bird} \end{cases}$$

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