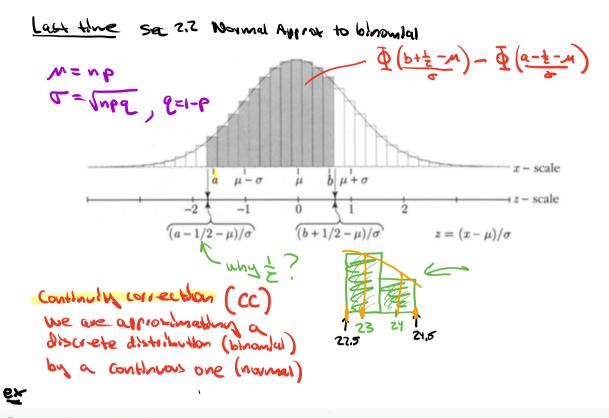
Stat 134 lec 6

Warmy

You coll a fair die 600 times.  
Using the normal distribution find the  
Chance you get between 74.5 and 75.5 sixes.  
Leave your answer in terms of 
$$\Phi$$
.  
 $M = np = 600(\frac{1}{6}) = 100$   
 $\sigma = 10pq = \sqrt{600(\frac{1}{6}\sqrt{56})} = 7.1$   
 $\Phi(\frac{75.5 - 100}{9.1}) - \Phi(\frac{74.5 - 100}{9.1}) = 0.00007$   
exact value  $P(k=75) = \binom{600}{75}\binom{1}{6}\binom{5}{6} = 0.0007$ 

Motivation: It is difficult to calculate exact probabilities with the binomial formula. It is easier to calculate the area under the normal curve.

245 25 75.5



Suppose that each of 300 patients has a probability of 1/3 of being helped by a treatment independent of its effect on the other patients. Find approximately the probability that more than 134 patients are helped by the treatment. (Be sure to use the continuity correction. You will not receive full credit otherwise)

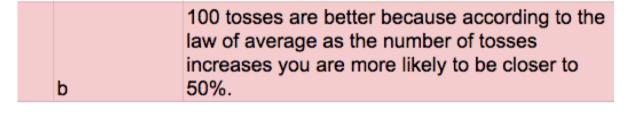
High The mean of 
$$Bin(n,p)$$
 is  $M = np$   
The should all deviation of  $Bin(np)$  is  $T = 1/pppp$   
 $n = 300$   
 $P = \frac{1}{3}$   
 $M = np = 300(\frac{1}{3}) = 100$   
 $\delta = (np q) = \sqrt{300(\frac{1}{3})(\frac{2}{3})} = \sqrt{\frac{200}{3}}$   
 $\chi = 4 \text{ pathents helped}$   
 $P(X \ge 134,5) = 1 - P(X < 139.5) = 1 - \frac{Q}{134, 5 - 100}$   
 $\sum_{i=1}^{100} \frac{134, 5 - 100}{\frac{1}{3}}$   
 $E(-1 = 0)$ 

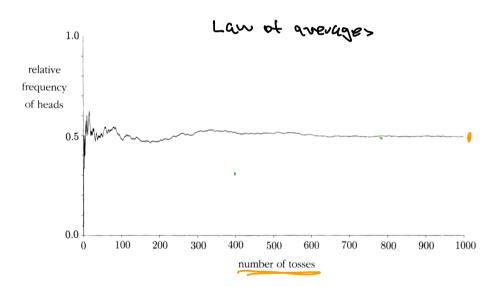
## () Concept test

. A fair coin is tossed, and you win a dollar if there are exactly 50% heads. Which is better?

a 10 tosses

 ${\bf b}$  100 tosses





Std dev is higher for n=100 so you are less likely to land exactly on 50% heads after 100 tosses compared to 10

Twoay

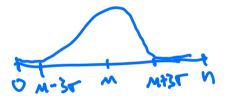
а

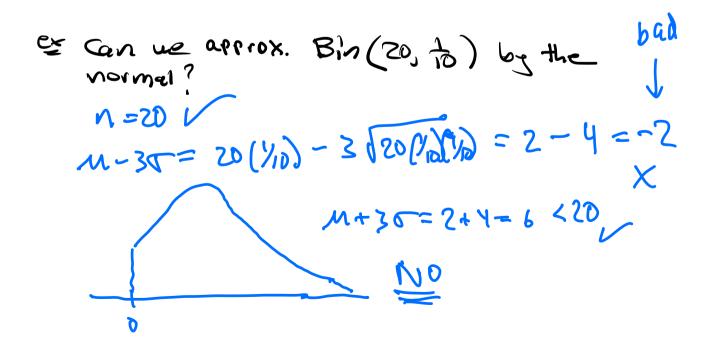
() Finith sec 2.2 (2) sec 2.4 Pobson approximation (skip sec 2.3)

(1) Sec 2.2 Normal approximation to the bihomilal distribution

For what NP is it of to approximate Bin (np) by a normal distribution N(M, r<sup>2</sup>) NZ20 share for fixed P, to bloom/at is more normal shaped as n'ncreases. (CLT) Outcomes of Bin (n, P) are 0,1,2,..,N 99.7% of our data is between M±35 more normal distributions

50 M-3070 and M+30 < M





tinyurl.com/jan30-2023



## stat 134 concept test

September 7 2022

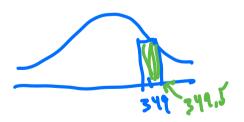
Southwest overbooks its flights, knowing some people will not show up. Suppose for a plane that seats 350 people, 360 tickets are sold. Based on previous data the airline claims that each passenger has a 90% chance of showing up. **Approximately**, what is the chance that at least one empty seat remains? (There are no assigned seats)

a) 
$$P(Z < \frac{350.5 - \mu}{\sigma})$$
  
b)  $P(Z < \frac{349.5 - \mu}{\sigma})$   
c)  $P(Z < \frac{360.5 - \mu}{\sigma})$   
 $T = \sqrt{q} = \sqrt{360(-q)} - 379$ 

d) none of the above

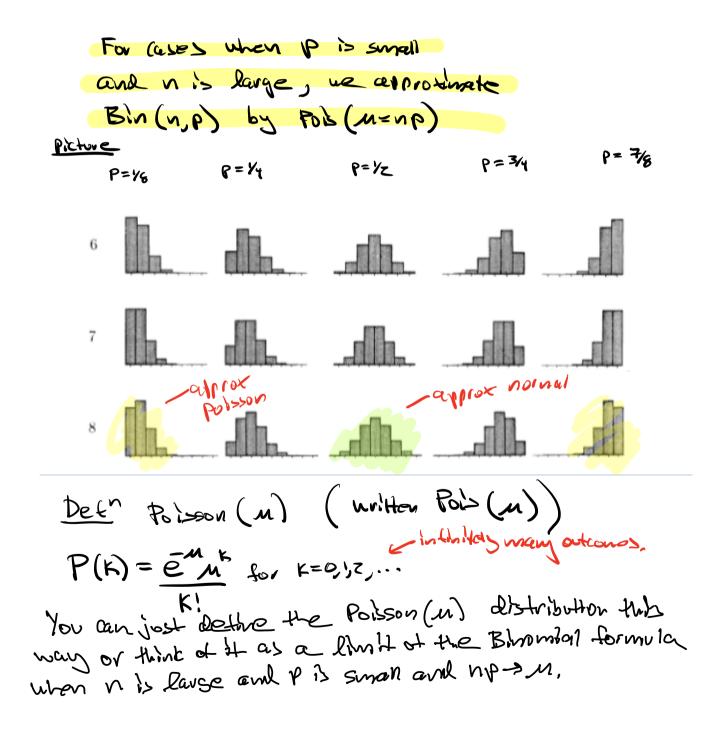
M+35 < N and 324-3570 and n= 360 720

X = # propile who show typ  $P(X \leq 349) \approx P(X \leq 349.5) = P(2 \leq \frac{349.5 - M}{5})$ 



(2) Sec 2.4 (skip 2.3) Poisson approx to Binowial

The normal enroximation has almost 100% of data ±35 from the mean M. For this reason we approximated the binomial wither normal only when ME35 is between O and N.



Then the proven in expendic at one at lecture notes,  
Then the proven in expendic at one at lecture notes,  

$$R(k)(k) p^{k}(1,p) \longrightarrow e^{-kk}$$
 as  $n \ge \infty$  and  $p \ge 0$   
 $F!$  with  $Np \Rightarrow M$   
 $F = E_{ch} = 500$  times, independently, on a bet with  $1000$   
Approximate the Chance of winning at head ence,  
Dont use at chance of winning at head ence,  
 $Dont use construction is discrete:$   
 $K = k both you why  $D = K^{n}$  P(K) =  $e^{-kk}$  for  $K = 0, K^{n}$ .  
 $F(K \ge 1) = 1 - P(K=0)$   $M \cong MP(K) = e^{-kk}$  for  $K = 0, K^{n}$ .  
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 $F(K \ge 1) = 0, K^{n} = 0$ .  
 $F(K \ge 1) =$$ 

P longe  
== 97.8% of approx 30 million poor families in the  
US. have a fulder. If you randomly sample 100  
of these families roughly what is the chance 98 or  
more have a fulder? Det Poisson (a)  

$$P = .978$$
  
 $N = 100$  success  
 $P(R) = \frac{e^{-M}}{K!}$  for  $k=0.12$ ...  
 $P(R) = \frac{e^{-M}}{K!}$  for  $k=0.12$ ....  
 $P(R) = \frac{e^{-M}}{K!}$  for  $k=0.12$ ...  
 $P(R) = \frac{e^{-M}$ 

$$\frac{A_{mendative}}{Thm} \quad \text{let } P_{n}(\mathbf{r}) = \binom{n}{k} P_{n}(\mathbf{r}$$

Proof of fact(Z):  
Proof of fact(Z):  
Remember from sec ZI P85, 
$$\frac{P_{n}(k)}{P_{n}(k-1)} = \frac{(n-k+1)}{k} \frac{P}{2}$$
  
=)  $P_{n}(k) = P_{n}(k-1) \frac{(n-(k-1))P_{n}}{k} \frac{P}{2}$   
=  $P_{n}(k-1) \frac{(n-(k-1))P_{n}}{k} \frac{1}{2} \approx P_{n}(k-1) \frac{n}{k}$