Stat 134: Section 13 Adam Lucas Mar. 28th, 2022

Conceptual Review

- a. What are the different functions we have used to characterize (i.e., fully describe) distributions of random variables?
- b. What is an order statistics? What is a general strategy to find the distribution of  $X_{(1)}, X_{(n)}$

Problem 1

Suppose we have a random variable *X* with continuous and strictly increasing CDF  $F_X$ . Find the distribution of  $F_X(X)$ .

Problem 2

Let  $X_1, \ldots, X_n$  be independent random variables where  $X_i \sim Exp(\lambda_i)$ for  $i = 1, 2, \ldots, n$ . Find the density of  $Y = \min\{X_1, \ldots, X_n\}$  and  $Z = \max\{X_1, \ldots, X_n\}$ .